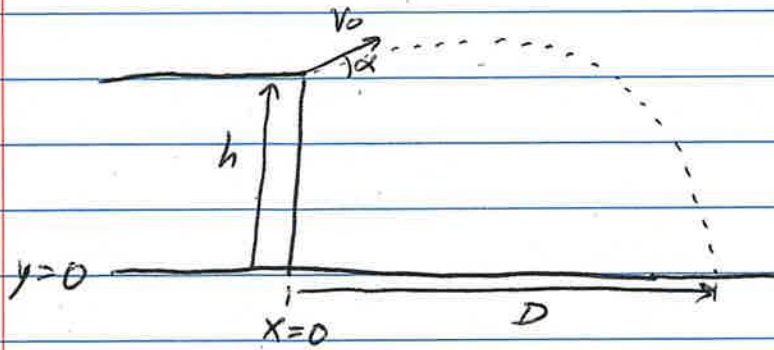


Range from Table Launch



$$V_{ox} = V_0 \cos \alpha \quad V_{oy} = V_0 \sin \alpha$$

$$y = h + V_{oy} t - \frac{1}{2} g t^2 \quad x = V_{ox} t$$

To find when the projectile lands, solve for t when $y = 0$

$$0 = h + V_{oy} t - \frac{1}{2} g t^2$$

$$0 = \frac{1}{2} g t^2 - V_{oy} t - h$$

$$t = \frac{V_{oy} \pm \sqrt{V_{oy}^2 + 2gh}}{g}$$

Passes units test

Passes sense test

Time to apex: $0 = V_y = V_{oy} - g t$

$$g t = V_{oy}$$

$$t = V_{oy} / g$$

This is the first term

Time to launch height = $2V_{oy} / g$ - solution when $h = 0$

Time to drop height h from rest: $0 = h - \frac{1}{2} g t^2$

$$g t^2 = 2h$$

$$t = \sqrt{2h/g} = \text{solution when } V_{oy} = 0$$

We can reject the negative solution bec it's before the launch

$$\text{Range } D = V_{ox} t = \frac{V_{ox}}{g} (V_{oy} + \sqrt{V_{oy}^2 + 2gh}) \text{ units work}$$

If you want to theoretically find maximum range, take the derivative of this formula with respect to launch angle α and find α at which $dD/d\alpha = 0$

If that's too difficult, numerically hunt for α giving the greatest D