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**PHYS 1210 Group Work Sheet**  
**Vectors in 3D**

With your group, discuss how to answer these questions and write your group answer in the space provided.

1. Define vectors  $\vec{A} = (10\hat{i} + 30\hat{j})$  N and  $\vec{B} = (0.50\hat{i} + 0.1\hat{j})$  m. What is the cross product of vectors  $\vec{A}$  and  $\vec{B}$ ?

2. A projectile's position after launch at time  $t = 0$  is given by the formula

$$\vec{r} = \left(15 \frac{m}{s} t\right) \hat{i} + \left(15 \frac{m}{s} t - 5 \frac{m}{s^2} t^2\right) \hat{j}.$$

- a. Its velocity is  $\vec{v} = d\vec{r}/dt$  and its acceleration is  $\vec{a} = d\vec{v}/dt$ . Find the projectile's velocity  $\vec{v}$  and acceleration  $\vec{a}$  as functions of time by taking the derivatives. Treat  $\hat{i}$  and  $\hat{j}$  as constants, because that's what they are.

- b. Sketch plots of the horizontal components of position, velocity, and acceleration vs. time.



- c. Sketch plots of the vertical components of position, velocity, and acceleration vs. time.



d. Find the formula for speed as a function of time,  $v = \sqrt{\vec{v} \cdot \vec{v}}$ .

e. Find the formula for magnitude of acceleration as a function of time.

f. Find the formula for rate of change of speed as a function of time,  $dv/dt$ .

3. Find the dot products between the unit basis vectors  $\hat{i}$ ,  $\hat{j}$ , and  $\hat{k}$ .

$$\hat{i} \cdot \hat{i} = \underline{\hspace{2cm}} \qquad \hat{i} \cdot \hat{j} = \underline{\hspace{2cm}} \qquad \hat{i} \cdot \hat{k} = \underline{\hspace{2cm}}$$

$$\hat{j} \cdot \hat{i} = \underline{\hspace{2cm}} \qquad \hat{j} \cdot \hat{j} = \underline{\hspace{2cm}} \qquad \hat{j} \cdot \hat{k} = \underline{\hspace{2cm}}$$

$$\hat{k} \cdot \hat{i} = \underline{\hspace{2cm}} \qquad \hat{k} \cdot \hat{j} = \underline{\hspace{2cm}} \qquad \hat{k} \cdot \hat{k} = \underline{\hspace{2cm}}$$

4. Find the cross products between the unit basis vectors  $\hat{i}$ ,  $\hat{j}$ , and  $\hat{k}$ .

$$\hat{i} \times \hat{i} = \underline{\hspace{2cm}} \qquad \hat{i} \times \hat{j} = \underline{\hspace{2cm}} \qquad \hat{i} \times \hat{k} = \underline{\hspace{2cm}}$$

$$\hat{j} \times \hat{i} = \underline{\hspace{2cm}} \qquad \hat{j} \times \hat{j} = \underline{\hspace{2cm}} \qquad \hat{j} \times \hat{k} = \underline{\hspace{2cm}}$$

$$\hat{k} \times \hat{i} = \underline{\hspace{2cm}} \qquad \hat{k} \times \hat{j} = \underline{\hspace{2cm}} \qquad \hat{k} \times \hat{k} = \underline{\hspace{2cm}}$$