
Worksheet 20: Pendulums

1. A torsional oscillator can be thought of as a torsion spring with torque constant κ and a rotor with moment of inertia I . Its kinematics follow an angular Hooke's law torque $\tau = -\kappa\theta$ and the angular Newton's second law $\tau = I\alpha$, where $\alpha = d^2\theta/dt^2$. Its angular displacement is given by the function $\theta = \cos(\omega t + \phi)$.

What is the value of ω in this function, in terms of the characteristics of the spring and rotor?

2. The small-angle approximation models $\sin \theta \approx \theta$ in radians. How small does θ need to be for this to be a decent approximation?

| θ | $\sin \theta$ | $\theta - \sin \theta$ | $(\theta - \sin \theta) / \sin \theta$ |
|--------------|---------------|------------------------|--|
| $1/180 \pi$ | | | |
| $2/180 \pi$ | | | |
| $5/180 \pi$ | | | |
| $10/180 \pi$ | | | |
| $20/180 \pi$ | | | |
| $45/180 \pi$ | | | |
| | | | 1% |
| | | | 5% |
| | | | 10% |

4. Find the length of a simple pendulum with a period of oscillation of 2.0 s.